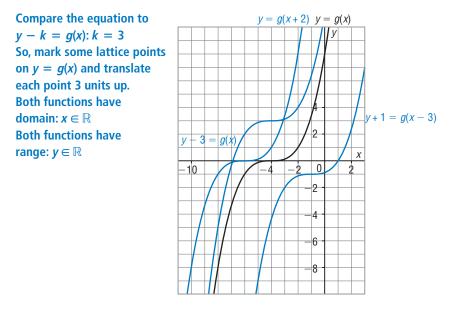
Checkpoint: Assess Your Understanding, pages 213–218

3.1

1. Multiple Choice The graph of $y = -3x^3 + 4$ is translated 4 units right and 5 units down. What is an equation of the translation image?

A. $y = -3(x + 4)^3 + 9$ **B.** $y = -3(x - 4)^3 + 9$ **C.** $y = -3(x + 4)^3 - 1$ **D.** $y = -3(x - 4)^3 - 1$ **2.** Here is the graph of y = g(x). On the same grid, sketch the graph of each function below. State the domain and range of each function.

a)
$$y - 3 = g(x)$$

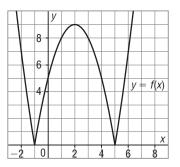


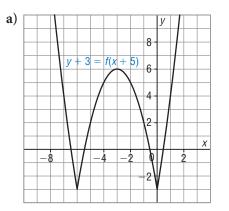
b) y = g(x + 2)

Write y = g(x + 2) as y = g(x - (-2)). Compare the equation to y = g(x - h): h = -2Translate each point on the graph of y = g(x) 2 units left. The domain is: $x \in \mathbb{R}$ The range is: $y \in \mathbb{R}$

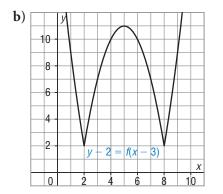
c) y + 1 = g(x - 3)

Write y + 1 = g(x - 3) as y - (-1) = g(x - 3). Compare the equation to y - k = g(x - h): h = 3 and k = -1Translate each point on the graph of y = g(x) 3 units right and 1 unit down. The domain is: $x \in \mathbb{R}$ The range is: $y \in \mathbb{R}$ **3.** The graph of y = f(x) was translated to create each graph below. Write an equation of each graph in terms of the function *f*.





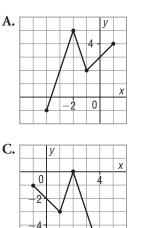
The graph of y = f(x) has a local maximum at (2, 9). This graph has a local maximum at (-3, 6). So, the graph of y = f(x) was translated 5 units left and 3 units down. The equation of the image graph has the form: y - k = f(x - h), where h = -5 and k = -3So, an equation of the image graph is: y + 3 = f(x + 5)

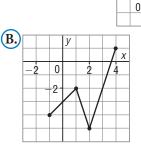


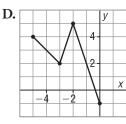
The graph of y = f(x) has a local maximum at (2, 9). This graph has a local maximum at (5, 11). So, the graph of y = f(x) was translated 3 units right and 2 units up. The equation of the image graph has the form: y - k = f(x - h), where h = 3 and k = 2So, an equation of the image graph is: y - 2 = f(x - 3)

3.2

4. Multiple Choice The graph of y = f(x) was reflected in the *x*-axis. Which graph below is its reflection image?







5. Here is the graph of y = k(x). On the same grid, sketch and label the graph of each function below, then state its domain and range.

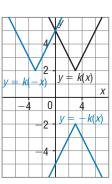
a)
$$y = -k(x)$$

The graph of y = -k(x) is the image of the graph of y = k(x) after a reflection in the x-axis. Mark some lattice points on y = k(x),

then reflect them in the x-axis. Mark these image points, then join them. **Domain**: $x \in \mathbb{R}$

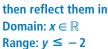
b) y = k(-x)

The graph of y = k(-x) is the image of the graph of y = k(x) after a reflection in the y-axis. Mark some lattice points on y = k(x), then reflect them in the *y*-axis. Mark these image points, then join them. **Domain**: $x \in \mathbb{R}$ Range: $y \ge 2$



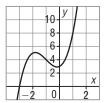
y = f(x)

Х



6. The graph of $y = -x^3 + 3x^2 - x + 3$ was reflected in the *y*-axis and its image is shown. What is an equation of the image?

When the graph of y = f(x) is reflected in the y-axis, the equation of its image is y = f(-x). So, an equation of the image is: y = f(-x) $y = -(-x)^3 + 3(-x)^2 - (-x) + 3$ $y = x^3 + 3x^2 + x + 3$



3.3

7. Multiple Choice The point (-6, 2) lies on the graph of y = f(x). After vertical and horizontal stretches or compressions of the graph, the equation of the image is y = 3f(2x). Which point is the image of (-6, 2)?

y = 2h(4x)

 $\frac{1}{3}h(-$

y = h(x)

8

A.(-3,6) **B.** (-12,6) **C.** (-2,4) **D.** (-18,1)

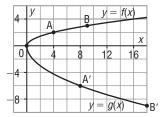
8. Here is the graph of y = h(x). On the same grid, sketch the graph of each function below, then state its domain and range. a) $y = \frac{1}{3}h(-2x)$

Compare y = ah(bx) to

 $y = \frac{1}{3}h(-2x)$: $a = \frac{1}{3}$ and b = -2So, the graph of y = h(x) is vertically compressed by a factor of $\frac{1}{3}$, horizontally compressed by a factor of $\frac{1}{2}$, then reflected in the *y*-axis. Use mental math and the transformation: (x, y) on y = h(x) corresponds to $\left(\frac{x}{-2}, \frac{1}{3}y\right)$ on $y = \frac{1}{3}h(-2x)$, to mark some image points, then join them. Domain: $-4 \le x \le 2$; range: $-1 \le y \le 2$

b) y = 2h(4x)

Compare y = ah(bx) to y = 2h(4x): a = 2 and b = 4So, the graph of y = h(x) is vertically stretched by a factor of 2, and horizontally compressed by a factor of $\frac{1}{4}$. Use mental math and the transformation: (x, y) on y = h(x) corresponds to $\left(\frac{x}{4}, 2y\right)$ on y = 2h(4x), to mark some image points, then join them. Domain: $-1 \le x \le 2$; range: $-6 \le y \le 12$ **9.** The graph of y = g(x) is the image of the graph of y = f(x) after a vertical and/or horizontal stretch and/or reflection. Corresponding points are labelled. Write an equation of the image graph in terms of the function *f*.



Point A(4, 2) on y = f(x) corresponds to point A'(8, -6) on y = g(x). An equation for the image graph after a vertical or horizontal stretch or compression can be written in the form y = af(bx).

A point (x, y) on y = f(x) corresponds to the point $\left(\frac{x}{b}, ay\right)$ on y = af(bx). The image of A(4, 2) is $\left(\frac{4}{b}, a(2)\right)$, which is A'(8, -6). Equate the x-coordinates: $b = \frac{1}{2}$ Equate the y-coordinates: a = -3So, an equation of y = g(x) is: $y = -3f\left(\frac{1}{2}x\right)$

I used the coordinates of B and B', and mental math to verify the equation.