**1. Multiple Choice** The graph of  $y + 2 = -3f(\frac{1}{2}(x + 5))$  is the image

of the graph of y = f(x) after several transformations. Which statement about how the graph of y = f(x) was transformed is false?

- **A.** The graph was reflected in the *x*-axis.
- **B.** The graph was horizontally stretched by a factor of 2.
- C. The graph was translated 2 units down.
- **D**. The graph was reflected in the *y*-axis.
- **2. Multiple Choice** Which statement about a function and its inverse is not always true?
  - A. The inverse of a function is a function.
  - **B.** The domain of a function is the range of its inverse, and the range of a function is the domain of its inverse.
  - **C.** The graph of the inverse of a function can be sketched by reflecting the graph of the function in the line y = x.
  - **D.** Each point (x, y) on the graph of a function corresponds to the point (y, x) on the graph of its inverse.
- **3.** Write an equation of the function  $y = \sqrt{x 3}$  after each transformation below.
  - a) a translation of 2 units right and 5 units down

The equation of the image graph has the form  $y - k = \sqrt{(x - h) - 3}$ , where k = -5 and h = 2. So, an equation of the image graph is:  $y + 5 = \sqrt{x - 5}$ 

**b**) a reflection in the *x*-axis

The *y*-coordinates of points on the graph of  $y = \sqrt{x - 3}$  change sign. So, an equation of the image graph is:  $y = -\sqrt{x - 3}$ 

**c**) a reflection in the *y*-axis

The *x*-coordinates of points on the graph of  $y = \sqrt{x-3}$  change sign. So, an equation of the image graph is:  $y = \sqrt{-x-3}$  **d**) a vertical stretch by a factor of 2 and a horizontal compression by a factor of  $\frac{1}{3}$ 

The equation of the image graph has the form  $y = a\sqrt{bx - 3}$ , where a = 2 and b = 3.

So, an equation of the image graph is:  $y = 2\sqrt{3x - 3}$ 

4. Here is the graph of y = f(x). On the same grid, use transformations to sketch the graph of y - 5 = -3f(2x). Describe the transformations.

Compare: y - k = af(b(x - h)) to y - 5 = -3f(2x) k = 5, a = -3, b = 2, and h = 0A point (x, y) on y = f(x) corresponds to the point  $\left(\frac{x}{b} + h, ay + k\right)$  on

y - k = af(b(x - h)).



Substitute the values above. A point on y - 5 = -3f(2x) has coordinates  $\left(\frac{x}{2}, -3y + 5\right)$ . Transform some points on the lines.

Point on $y = f(x)$	Point on $y - 5 = -3f(2x)$
(-4, 4)	(-2, -7)
(0, 0)	(0, 5)
(4, 4)	(2, -7)

Draw 2 lines through the points for the graph of y - 5 = -3f(2x). The graph of y = f(x) was compressed horizontally by a factor of  $\frac{1}{2}$ , stretched vertically by a factor of 3, reflected in the *x*-axis, then translated 5 units up.

- **5.** Here is the graph of  $y = \sqrt{x}$ .
  - **a**) Use this graph to sketch a graph of  $y 1 = -2\sqrt{\frac{1}{2}(x 4)}$ .



Compare: y - k = af(b(x - h)) to

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$$y - 1 = -2\sqrt{\frac{1}{2}(x - 4)}$$
  

$$k = 1, a = -2, b = \frac{1}{2}, \text{ and } h = 4$$
  
A point  $(x, y)$  on  $y = f(x)$  corresponds to the point  $\left(\frac{x}{b} + h, ay + k\right)$ 

on 
$$y - k = af(b(x - h))$$
.

Substitute the values above.

A point on  $y - 1 = -2\sqrt{\frac{1}{2}(x - 4)}$  has coordinates: (2x + 4, -2y + 1)Transform some points on  $y = \sqrt{x}$ .

Point on	Point on
$y = \sqrt{x}$	$y - 1 = -2\sqrt{\frac{1}{2}(x - 4)}$
(0, 0)	(4, 1)
(1, 1)	(6, -1)
(4, 2)	(12, -3)

Join the points with a smooth curve for the graph of  $y - 1 = -2\sqrt{\frac{1}{2}(x - 4)}$ .

**b**) Write the domain and range of the function in part a.

From the graph, the domain is  $x \ge 4$ ; and the range is  $y \le 1$ .

**6.** a) Determine an equation of the inverse of  $y = (x - 4)^2 + 5$ .

Interchange x and y in the equation.  $x = (y - 4)^2 + 5$  Solve for y.  $(y - 4)^2 = x - 5$   $y - 4 = \pm \sqrt{x - 5}$  $y = \pm \sqrt{x - 5} + 4$ 

**b**) Sketch the graph of the inverse. Is the inverse a function? Explain.



Graph  $y = (x - 4)^2 + 5$ . This is the graph of  $y = x^2$  after a translation of 4 units right and 5 units up. Interchange the coordinates of points on this graph, then plot the new points to get the graph of  $y = \pm \sqrt{x - 5} + 4$ . No, the inverse is not a function because its graph does not pass the vertical line test.

c) If your answer to part b is yes, explain how you know. If your answer to part b is no, determine a possible restriction on the domain of  $y = (x - 4)^2 + 5$  so its inverse is a function, then write the equation of the inverse function.

The domain can be restricted by considering each part of the graph of  $y = (x - 4)^2 + 5$  to the right and left of the vertex. So, one restriction is  $x \ge 4$  and the equation of the inverse function is:  $y = \sqrt{x - 5} + 4$ Another restriction is  $x \le 4$  and the equation of the inverse function is:  $y = -\sqrt{x - 5} + 4$